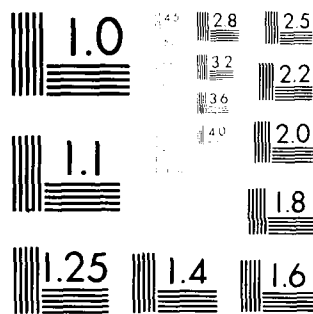


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Technical Report No. 39

DYNAMIC MIXED MODE FRACTURE

by

A. S. Kobayashi and M. Ramulu

August 1980

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DYNAMIC MIXED MODE FRACTURE

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Department of Mechanical Engineering, University of Washington

ABSTRACT

A newly developed data reduction process was used to reevaluate dynamic photoelastic results and to extract dynamic stress intensity factors, K_I^{dyn} and K_{II}^{dyn} , associated with curved and branched cracks in fracturing Homalite - 100 plates. A branching stress intensity factor approximately 5 times the fracture toughness was identified for this material. Moderate to severe crack curvings were associated with a K_I^{dyn} and K_{II}^{dyn} ratio as low as 0.05, but with positive remote stress component, σ_{ox} .

INTRODUCTION

Two dimensional dynamic photoelasticity has been used by Dally and his associates [1,2] and by the author and his associates [3,4] to determine experimentally the dynamic stress intensity factor K_I^{dyn} , surrounding a propagating crack and to establish a dynamic fracture toughness, K_{ID} , versus crack velocity \dot{a} , relation which may control dynamic fracture. This use of dynamic photoelasticity in studying dynamic fracture has been eloquently described by J. W. Dally in his recent article [1]. As noted by Dally, the data reduction procedure used by most investigators in the past for calculating K_I^{dyn} , from the transient isochromatics surrounding the propagating crack tip, was restricted to Mode I crack tip deformation. A theoretical, near-field, static isochromatics was first equated to the recorded experimental dynamic isochromatics and the resultant static stress intensity factor of the former was considered the dynamic stress intensity factor of the latter [2,5]. Error estimates for using a near-field stress to extract the Mode I dynamic stress intensity factor have been made by several investigators [6-8] and in particular, exhaustively by Rossmanith and Irwin [8].

Studies of the static isochromatic patterns under mixed mode loading conditions, i.e. in the presence of combined K_I and K_{II} crack tip deformations were made by C. W. Smith [9,10], Gdousto and Theocaris [11] and more recently by Dally and Sanford [12,13] and Rossmanith [14]. These mixed mode isochromatics are all characterized by their unsymmetric patterns with respect to the straight crack line. It is also interesting to note that the shapes of these static isochromatics are strongly influenced by the higher order terms, i.e. terms other than K_I and K_{II} . In particular, the second order term of σ_{ox} , commonly referred to as the remote stress component, will distort the symmetry of the isochromatics by significant stretching and

shortening of the upper and lower loop system [14]. For a pure mode II crack tip deformation, the isochromatic loop straddles the crack tip as shows in Figure 1 where a nearly pure shear state of stress is generated around branched cracks. The mode II stress intensity factors K_{II} , and remote stress components σ_{ox} , associated with these isochromatics are listed in the following Table 1.

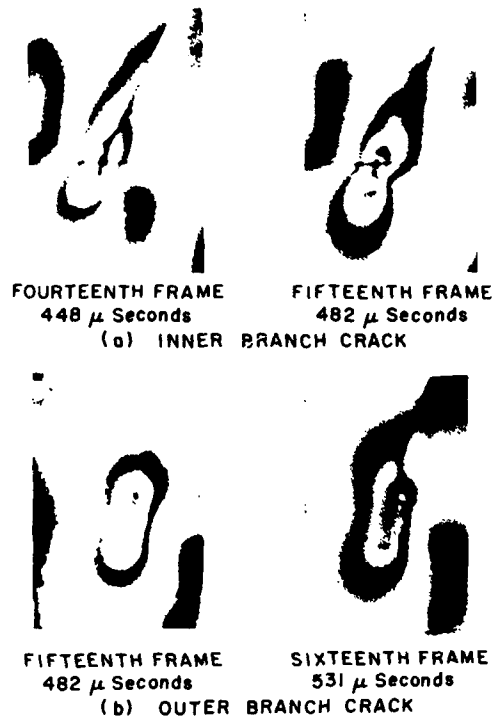


Fig. 1 Typical Mode II Dynamic Isochromatic Patterns of Arresting Branched Cracks. Homalite-100 Single Edge Notched Specimen Under Fixed-Grip Loading. Specimen No. B5

Table 1. K_{II} and σ_{ox} for Arrested Branch Cracks in Fig. 1

(a) Inner Branch Crack

	14th Frame	15th frame
K_{II}	0.4 MPa \sqrt{m}	0.44 MPa \sqrt{m}
σ_{ox}	0.32 MPa	-0.04 MPa

(b) Outer Branch Crack

	15th frame	16th frame
K_{II}	0.44 MPa \sqrt{m}	0.41 MPa \sqrt{m}
σ_{ox}	0.18 MPa	0.08 MPa

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In actual dynamic photoelastic analysis of dynamic fracture, dynamic isochromatics surrounding a running crack often exhibits moderate unsymmetry but such photoelastic patterns were heretofore considered experimental abnormalities and were ignored by averaging the unsymmetric patterns during the data reduction process. Careful postmortem inspection of the fracture specimens, however, show that the slightly unsymmetric isochromatics are often associated with slightly curved crack paths which undoubtedly are caused by the small dynamic K_{II}^{dyn} , coexisting with the dominating dynamic K_I^{dyn} value. This effect is akin to the small but noticeable influence of a small K_{II} on fatigue crack propagation reported fifteen years ago [15]. The exact relation between the amount of crack curving and the dynamic K_I and possibly other higher order terms of the near field stresses associated with the propagating crack tip would thus provide a dynamic crack propagation law under mixed-mode crack tip deformation similar to the K_{ID} versus \dot{a} relation under consideration for Mode I dynamic crack propagation.

With the development of a data reduction procedure for evaluating K_{II}^{dyn} together with K_I^{dyn} values, it became possible to investigate experimentally the role of mixed mode dynamic near field stresses in dynamic fracture. The authors used such procedure to evaluate the stress intensity factors associated with crack branching and crack curving [16]. The purpose of this paper is to use this data reduction procedure to further extract K_I^{dyn} and K_{II}^{dyn} from the previously recorded dynamic isochromatics surrounding running crack tips of curved and branched cracks.

DATA REDUCTION PROCEDURE

A three parameter, mixed mode, near-field state of stresses surrounding a crack propagating at constant velocity [17,18] was used to derive a relation between the Modes I and II dynamic stress intensity factors, K_I^{dyn} and K_{II}^{dyn} , and the remote stress component σ_{ox} , and the dynamic isochromatics. This relation together with an overdeterministic, least-square method formed the basis of a data reduction procedure for extracting the three dynamic parameters K_I^{dyn} and K_{II}^{dyn} and σ_{ox} from the recorded dynamic photoelastic pattern surrounding a running crack. Further details of this data reduction procedure can be found in Reference [16].

Figure 2 shows two frames out of a 16-frame dynamic photoelastic record of a curving crack in a notch bend specimen 9.58mm (3/8 inch) thick, 88.9 x 400mm (3 1/2 x 15 3/4 inch) Homalite-100 beam with a blunt initial crack of 6.4mm (7/32 inch) in length and which was impact loaded by a drop weight of 1.48 kg (3.25 lbs) [19]. The crack emanated from the blunt saw-cut pre-crack and propagated through much of the height of the beam prior to curving as it approached the region of impact loading. Further details of the experimental setup, crack velocity measurements and dynamic calibration of the Homalite-100 material used are found in Reference [19]. Figure 3 shows the K_I^{dyn} and K_{II}^{dyn} and σ_{ox} variations obtained from the dynamic photoelastic patterns preceding and immediately after the crack curving shown in Figure 2. The negligible K_{II}^{dyn} with respect to the K_I^{dyn} leads to speculation that the important factor governing the crack curving is not the K_{II}^{dyn} component of the mixed mode local dynamic state of stress, but rather the σ_{ox} component which heretofore was ignored in past static analyses. The directional sta-

bility of the static Mode I crack extension with σ_{ox} as a dominant factor, however, has been presented recently [20] and thus it is conceivable that the second order term, i.e. σ_{ox} in the dynamic near-field stresses, may also govern the crack path of a rapidly propagating crack. Crack curving associated with the large positive σ_{ox} values in Fig. 3 tends to confirm this speculation.

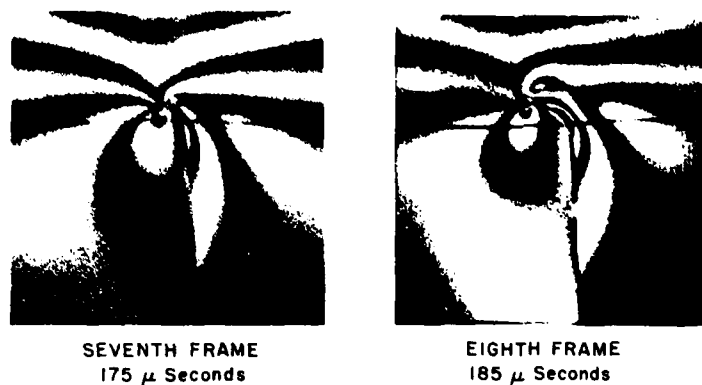


Fig. 2 Typical Dynamic Isochromatics of a Curved Crack. Homalite-100 notch bend specimen. Specimen No. 1-C042574

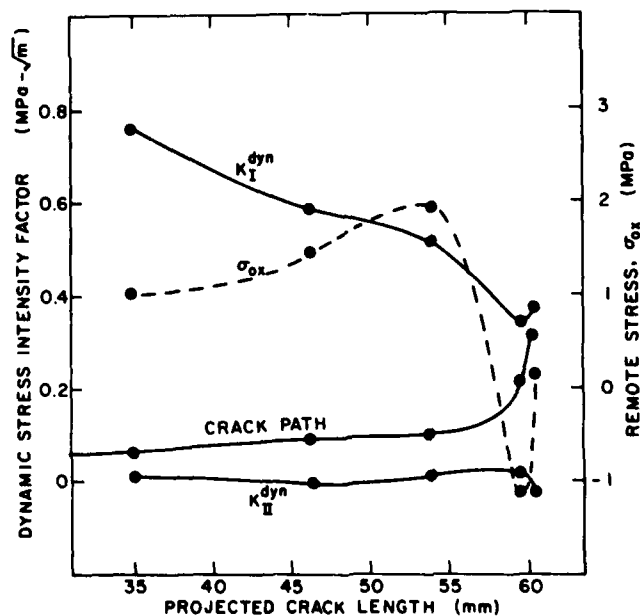


Fig. 3 Modes I and II Dynamic Stress Intensity Factors of the Curved Crack Shown in Fig. 2.

Figure 4 shows a slightly slanted crack and the associated K_I^{dyn} , K_{II}^{dyn} and σ_{ox} in a fracturing, wedge-loaded, double cantilever beam specimen of 9.6mm (3/8 inch) thick, 76.2 x 152.4mm (3 x 6 inch) Homalite-100 plate. Details of this experimental setup, etc., can be found in Reference [21]. Some fluctuations in K_I^{dyn} and K_{II}^{dyn} throughout the crack propagation history is noted. Again, the consistently low K_{II}^{dyn} values and the large positive σ_{ox} associated with significant crack curving tend to verify the previous finding regarding the importance of σ_{ox} in dynamic crack curving. It appears then that a fracture dynamic theory comparable to that of Ref. [20] and in the presence of small but non-negligible K_{II}^{dyn} may provide insight to dynamic crack curving.

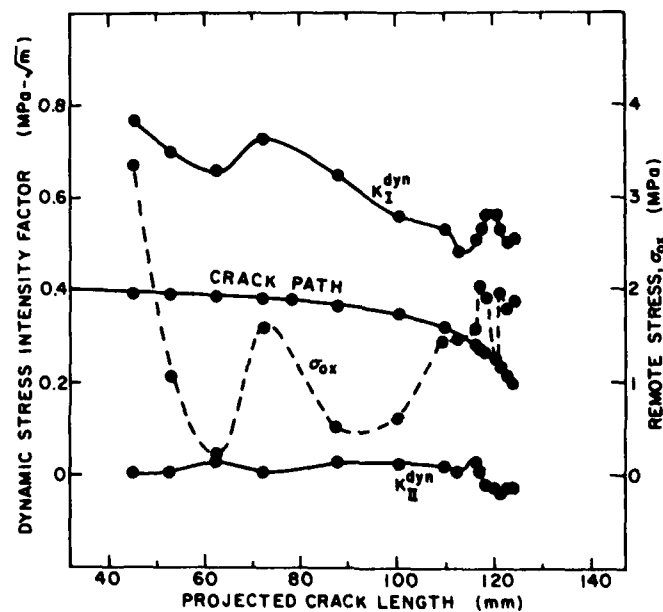


Fig. 4 Modes I and II Dynamic Stress Intensity Factors of a Slanted Crack in a Wedge-Loaded Rectangular Double Cantilever Specimen. Homalite-100 Specimen No. L31S-030274.

Figure 5 shows two dynamic photoelastic patterns of a branched crack in a single edge-notched 9.5mm (3/8 inch) thick, 254 x 254mm (10 x 10 inch) Homalite-100 plate subjected to fixed grip loading condition. Other branched cracks from this same specimen were shown in Fig. 1 and the experimental details of this test can be found in Reference [2]. As shown in Fig. 5, within the 49 micro-second interval, the propagating crack turned about 74° and arrested. The mixed Mode stress intensity factors prior to this severe crack kinking were $K_I^{dyn} = 0$, $K_{II}^{dyn} = 0.41 \text{ MPa}\sqrt{\text{m}}$ and $\sigma_{ox} = 0.18 \text{ MPa}$. After crack kinking at which time the crack arrested, $K_I = 0.34 \text{ MPa}\sqrt{\text{m}}$, $K_{II} = 0.08 \text{ MPa}\sqrt{\text{m}}$ and $\sigma_{ox} = 1.4 \text{ MPa}$. This severe crack curving, i.e. crack kinking can also occur under the more traditional high K_{II} state of stress.

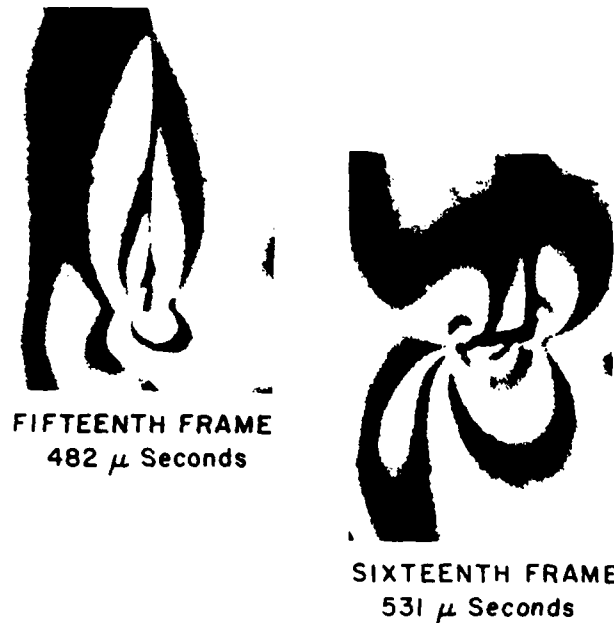


Fig. 5 Dynamic Isochromatics Prior To and After Crack Kinking. Homalite-100 Single Edge Notched Specimen Under Fixed Grip Loading. Specimen No.B5

The above three sets of data are obviously not sufficient to establish a dynamic crack curving criterion. Quantitative correlation of k_{dyn} , k_{dyn} and σ_{ox} with the degree of crack curving as well as the possible dependence on crack velocity are lacking at this time.

CRACK BRANCHING

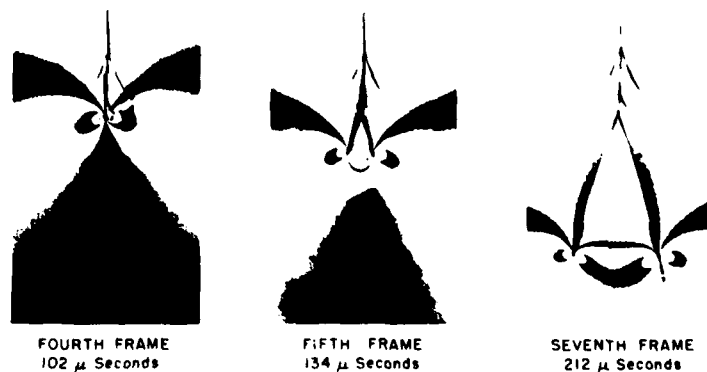


Fig. 6 Typical Crack Branching Dynamic Photoelastic Patterns Homalite-100 Single Edge Notched Specimen (Fixed Grip Loading) Specimen No. B8.

Figure 6 shows three frames out of a 16-frame dynamic photoelastic record of a crack propagating and branching in a 3.2mm (1/8 inch) thick, 254 x 254mm (10 x 10 inch) Homalite-100 plate loaded under fixed grip tension. Details of the experiment can be found in Reference [22].

Figure 7 shows the K_I^{dyn} and K_{II}^{dyn} for two branches of the cracks shown in Figure 6. By extrapolating the K_I^{dyn} associated with two branch cracks, an after-branching $K_I^{dyn} = 1.2 \text{ MPa } \sqrt{\text{m}}$ (10.90 psi $\sqrt{\text{in.}}$) and $K_{II}^{dyn} = 0.45 \text{ MPa } \sqrt{\text{m}}$ (410 psi $\sqrt{\text{in.}}$) are obtained. The branching stress intensity factor, i.e. immediately prior to branching, is estimated to be $K_I^{dyn} = 2.03 \text{ MPa } \sqrt{\text{m}}$ (1850 psi $\sqrt{\text{in.}}$).

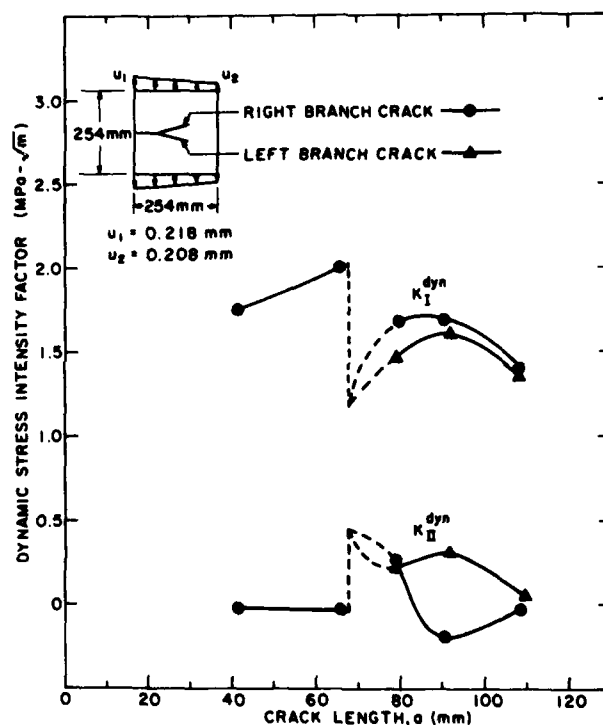


Fig. 7 Modes I and II Dynamic Stress Intensity Factors of the Branched Cracks Shown in Fig. 6.

Figure 8 shows another set of K_I^{dyn} and K_{II}^{dyn} for two branch cracks in a similar dynamic photoelastic experiment [20]. By extrapolating the K_I^{dyn} associated with the only readable right branch data, an after branching $K_I^{dyn} = 1.02 \text{ MPa } \sqrt{\text{m}}$ (920 psi $\sqrt{\text{in.}}$) and $K_{II}^{dyn} = -0.2 \text{ MPa } \sqrt{\text{m}}$ (180 psi $\sqrt{\text{in.}}$) are obtained. The extrapolated dynamic stress intensity factors prior to branching are $K_I^{dyn} = 2.03 \text{ MPa } \sqrt{\text{m}}$ (1850 psi $\sqrt{\text{in.}}$) and $K_{II}^{dyn} = 0$.

The average branching and after-branching stress intensity factors of the above two experiments as well as those for the single experiment reported in Reference [15] yield the following:

Branching $K_I^{dyn} = 2.03 \text{ MPa } \sqrt{\text{m}}$ (1850 psi $\sqrt{\text{in}}$)

$K_{II}^{dyn} \doteq 0$

After Branching $K_I^{dyn} = 1.0 \text{ MPa } \sqrt{\text{m}}$ (950 psi $\sqrt{\text{in}}$)

$K_{II}^{dyn} = 0.2 \text{ MPa } \sqrt{\text{m}}$ (180 psi $\sqrt{\text{in}}$)

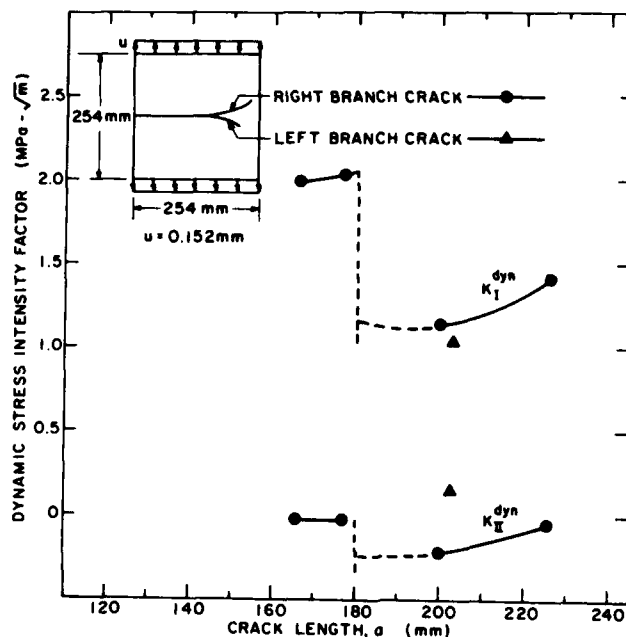


Fig. 8 Model I and II Dynamic Stress Intensity Factors of a branched Crack in a Homalite-100 Single Edge Notched Specimen Under Fixed Grip Loading. Specimen No. B9.

The above branching K_I^{dyn} data is identical to that quoted in Reference [1]. The ratio of before over after K_I^{dyn} of $2.03/1.0 \doteq 2.0$ is consistent with the postulate that crack branching occurs to dissipate fracture energy along two propagating cracks but is higher than the expected $\sqrt{2}$ value. It is also interesting to note that K_{II}^{dyn} which is prior to crack branching regains a small magnitude immediately after crack branching and is consistent with the static results of Reference [23].

DISCUSSIONS

The above dynamic photoelastic data on crack curving and crack branching should be considered as preliminary since the data is not sufficient in quantity for establishing a dynamic crack curving or a crack branching criteria. Evaluation of the accumulated dynamic photoelastic experiments using the newly developed data reduction procedure is continuing and the new crack curving and crack branching dynamic photoelastic experiments are planned.

ACKNOWLEDGEMENT

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